

# Year 13 Further Mathematics Mock Set#02b

## Further Mechanics FM1

- Advised to print in “A3-booklets”, this will allow all questions to be on the left hand side.
- You can also print in A4, double-sided, and two staples on the left
- If instead you print in 2-in-1 settings, first print the second page up to the last page, then print the cover page separately (to allow all questions on the left)

This exam paper has 7 questions, for a total of 75 marks.

| Question | Marks | Score |
|----------|-------|-------|
| 1        | 10    |       |
| 2        | 6     |       |
| 3        | 9     |       |
| 4        | 8     |       |
| 5        | 12    |       |
| 6        | 17    |       |
| 7        | 13    |       |
| Total:   | 75    |       |









































6.

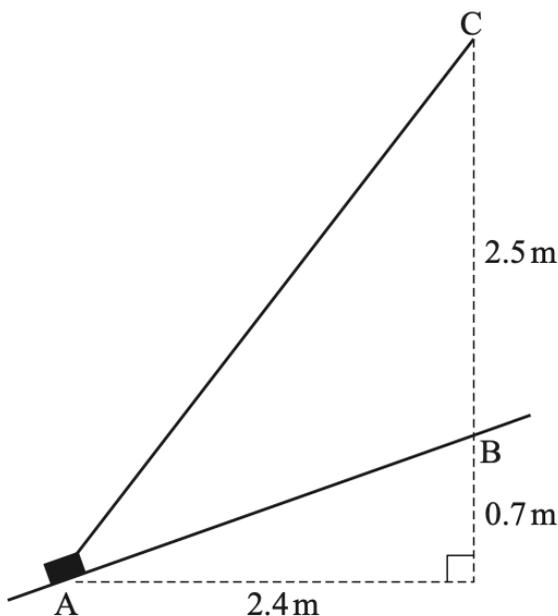


Figure 3

The fixed points  $A$  and  $B$  lie on a line of greatest slope of a smooth inclined plane, with  $B$  higher than  $A$ . The horizontal distance from  $A$  to  $B$  is  $2.4$  m and the vertical distance is  $0.7$  m. The fixed point  $C$  is  $2.5$  m vertically above  $B$ , as shown in Figure 3.

A light elastic string of natural length  $2.2$  m has one end attached to  $C$  and the other end attached to a small block of mass  $9$  kg which is in contact with the plane. The block is in equilibrium when it is at  $A$ .

- (a) Show that the modulus of elasticity of the string is  $37.73$  N. (5)

The block starts at  $A$  and is at rest. A constant force of  $18$  N, acting in the direction  $AB$ , is then applied to the block so that it slides along the line  $AB$ .

- (b) Find the magnitude and direction of the acceleration of the block
- (i) when it leaves the point  $A$ ,
  - (ii) when it reaches the point  $B$ . (6)
- (c) Find the speed of the block when it reaches the point  $B$ . (6)

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7.

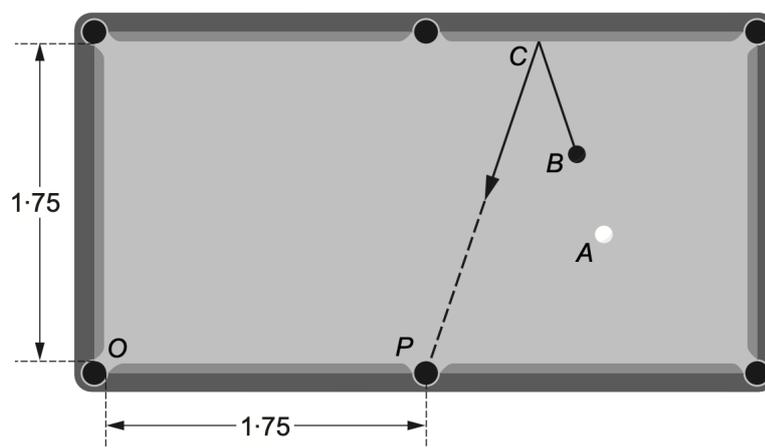


Figure 4

Ronnie “The Rocket” O’Sullivan is playing a game of snooker. The dimensions of the table, in metres, are shown in Figure 4.

The snooker table is modelled as a horizontal  $x$ - $y$  plane with the point  $O$  as the origin. The table and the four sides, called cushions, are modelled as smooth surfaces. Unit vectors parallel to the  $x$ -axis and the  $y$ -axis are denoted by  $\mathbf{i}$  and  $\mathbf{j}$  respectively. All balls on the table have a common mass  $m$  kg.

Initially, all balls are stationary.

Ronnie strikes the ball  $A$  so that it collides with ball  $B$ .

Before the collision,  $A$  has velocity  $(-\mathbf{i} + 8\mathbf{j}) \text{ ms}^{-1}$  and, after the collision, it has velocity  $(2\mathbf{i} + \mathbf{j}) \text{ ms}^{-1}$ .

(a) Show that the velocity of ball  $B$  after the collision is  $(-3\mathbf{i} + 7\mathbf{j}) \text{ ms}^{-1}$ . (3)

After the collision with ball  $A$ , ball  $B$  hits the cushion at point  $C$  before rebounding and moving towards the pocket at  $P$ .

The cushion is parallel to the vector  $\mathbf{i}$  and the coefficient of restitution between the cushion and ball  $B$  is  $\frac{5}{7}$ .

(b) Calculate the velocity of ball  $B$  after impact with the cushion. (3)

(c) Find, in terms of  $m$ , the magnitude of the impulse exerted on ball  $B$  by the cushion at  $C$ , stating your units clearly. (3)

Given that  $C$  has position vector  $(x\mathbf{i} + 1.75\mathbf{j}) \text{ m}$ .

(d) (i) Determine the time taken between the ball hitting the cushion at  $C$  and entering the pocket at  $P$ .  
 (ii) Find the value of  $x$ . (4)











